Abstract
Clustering a power system is very useful for the purpose of voltage stability control. However, the methods have developed usually have computational inefficiency. This paper presents a new cluster bus technique using Kohonen neural network for the purpose of forming bus clusters in power systems from the voltage stability viewpoint. This cluster formation will simplify voltage control in power system. With this proposed Kohonen algorithm, a large bus system will be partitioned into a small bus groups that have a coherence $V, \theta, P$ and $Q$. The maximum number of area clusters will be formed need for voltage stability needed. The proposed technique was tested on IEEE 39 bus system by considering two contingency namely load increased and line outage by using voltage collapse analysis. This formation will be compared with the Learning Vector Quantization (LVQ) algorithm. The results showed the proposed technique produces four clusters on contingency load load increased and three clusters online outage contingency on IEEE 39 bus system as shown by the LVQ.

Keywords: clustering, Kohonen, learning vector quantization, voltage stability

1. INTRODUCTION
Voltage stability is concerned with the ability of the power systems to maintain acceptable voltages at all system buses under normal conditions as well as after being subjected to a disturbance. For the system to remain secure in real time situation, it is essential to monitor the system status with respect to load changes and contingencies and take preventive action every time a contingency drives the system towards insecure state [1]. Voltage instability phenomenon has been known to be caused by heavy loads where large amounts of real and reactive powers are transported over long transmission lines. It may occur at the operating loading condition when a system is subjected to a contingency. The probability for a system to experience a voltage collapse resulting from the voltage instability condition is higher for weak areas or non-secure buses [2], [3]. Voltage instability incidence and hence power blackout can be avoided if identification of weak areas in a power network and voltage control are taken into account [2]-[4]. The need for fast control action so as to improve voltage stability calls for the formation of bus clusters or groups of buses in a power network. This is important because the information can be used for voltage control scheme in order to maintain power delivery to utility. The coherent bus clusters are formed in which the buses in a cluster are said to be coherent when the voltage and angle changes for these buses are the same for a particular contingency. Each cluster can therefore represent a group of coherent PV or PQ buses so as to form one sub-network of a large network [5]-[7]. By forming several sub-networks representing the entire power system, the size of the system can be reduced and therefore the computational efficiency of application program such as voltage control can be considerably improved. In this paper, the method for forming bus clusters is presented using a new clustering technique based on Kohonen neural network.

Many works have been carried out on bus clustering, for instance in voltage stability analysis where the sensitive lines in a system during stressed condition are identified and based on these lines the bus clusters are formed [2]. Clustering is also referred as a weak area partitioning which is determined based on the reduced load flow Jacobian determinant [6].
this work, the weak areas are clustered by encircling the load and generator buses that are
connected close to the critical bus. In [7], bus clusters are formed by utilizing the line stability
factors for voltage stability analysis. A power network can be clustered into smaller networks
containing buses that are closely connected [3], [8]. A group of load buses that have similar
voltage and angle change are considered as electrically belonging to the same cluster. On the
other hand, for load buses with voltages and angles not affected by load variations are
considered as electrically distanced or weakly connected and therefore belong to different
clusters [3], [8].

This paper presents the development of a new clustering technique using the
Kohonen neural network for determining the bus clusters in power systems. The objective of
the work is to form bus clusters in a power system based on the coherency of the buses. In
the proposed technique, a disturbance is first created at a particular bus such as load
increase or line outage. The coherent bus clusters are formed by considering values of
voltage difference, angle difference, real and reactive power differences which are similar for
buses within a cluster. In other words, the coherent buses that are grouped into a cluster are
said to have similar voltage and angle changes as well as real and reactive power changes.
Unsupervised learning method based on Kohonen neural network is also used to form the bus
clusters by giving a good representation on the characteristic groups from the input data space
[3]-[5], [9]. The proposed clustering technique was implemented on the IEEE 39-bus test
system.

2. PROPOSED METHOD

The bus clusters are formed based on the coherent nature of buses in a smaller cluster
by using the sensitivity information such as voltage magnitude and angle as well as real and
reactive power differences. A bus that tolerates a higher increase in load is considered less
sensitive as compared to a bus which tolerates a lower increase in load from its base load [10].
In order to create the cluster buses the Kohonen neural network will be proposed. The proposed
method is described as follow.

2.1. Kohonen Neural Network

Kohonen network is an unsupervised neural network in which its input data with
similar features are mapped to form clusters by competitive learning algorithm. The
algorithm considers the Euclidean distance between two n-dimensional vectors which is
measured by the similarity between input vectors. The distance of an input vector from each
neuron i, $D_i$ is given by,

$$D_i = \left\| W_{ij} - X \right\| = \sqrt{\sum_{j=1}^{n} (x_j - w_{ij})^2} \quad (1)$$

where $X = (x_1, x_2, ... x_n)^T$ denotes an input vector

$w_i = (w_{i1}, w_{i2}, ... w_{im})^T$ denotes the weight vector of the i-th neuron

The Kohonen with a minimum distance is called as the winner. In other words, the
winner’s weight vector is closest to the input vector.

$$D_w = \min \{ D_i \} \quad i \in \{1,2,\ldots,m\} \quad (2)$$

In the Kohonen algorithm, the concept of the winner-take-all units are related to the
biological concept of grandmother cells because they are responsible for selecting one
specific feature, for example, the feature presenting the stereotypical grandmother.
However, this representation is not robust because when one unit is removed; all information
concerning the corresponding class would be lost. For robust competitive learning, Kohonen
proposed the self organizing training algorithm. Ideally neighboring neurons classify
neighboring features and thus the loss in one neuron will result in a decrease of accuracy
but not in a complete loss of information [11]. For each input vector only one such unit will
respond, namely the unit characterized by the maximum output, respectively minimum distance, for this input vector \( x \). During the training, the winner adjusts its weights to be closer to the values of data and the neighbours of the winner also adjust their weights to be closer to the same input data vector according to the following relation [12],

\[
W_i = W_i + \alpha(W_i - X) \quad i = \{1, 2, \ldots, m\}
\]

The units of the network are thus competing for selection. Only the weights of the winner will be adapted. The adjustment of the neighbouring neuron is instrumental in preserving the order of the input data. Thus, the winning neuron is the closest to the input value. After training, the weight vectors are self-organizing and represent prototypes of classes of input vector [13]. The complete algorithm is described as follows:

1. \( t := 1 \); initialize \( w_{ij} \) randomly for \( i = 1, \ldots, m \); \( j = 1, \ldots, n \),
   Initialize weight of bias \( b_i = e^{[1 - \ln(K_i)]} \),
   where \( b_i \) is bias weight neuron-\( i \) and \( K \) is amount of class.
   Set learning rate and maximum epoch.
2. Choose input vector \( x \in X \) randomly in the training set.
3. Determine the neuron \( i \) such that its weight vector \( w \) is closest to the input vector.
   \( D_i = \min \{D_i\} \quad i \in \{1, 2, \ldots, m\} \) for all \( i \)
4. Update the weight vector \( w_{ij} = 1, \ldots, m \); \( i = 1, \ldots, m \),
   \( W_i = W_i + \alpha(W_i - X) \quad i = \{1, 2, \ldots, m\} \)
5. Update bias weight:
   \( c(i) = (1 - \alpha)e^{[1 - \ln(b(i))] + \alpha y(i)} \) for the winner neuron
   \( b(i) = e^{[1 - \ln(c(i))]}) \) for else
6. Increment the time \( t := t + 1 \)
7. Go to step (ii) until maximum epoch is reached.

2.2. Learning Vector Quantization

A supervised version of the Kohonen algorithm known as the learning vector quantization (LVQ) is also introduced by Kohonen [14]. In this algorithm, it is assumed that for each training vector \( x \), the class is known. Using this knowledge, the weight vectors can be moved, that is, the class prototypes move towards a correctly classified training vector and away from a wrongly classified one. The LVQ algorithm is described as follows:

1. \( t := 1 \); initialize weight input variable-\( j \) to cluster-\( i \) \( w_{ij} \)
   randomly for \( i = 1, \ldots, m \); \( j = 1, \ldots, n \),
   Set maximum epoch, Learning rate (\( \alpha \)), Decrease learning rate (\( \text{deca} \)) and minimum learning rate (\( \text{min} \alpha \))
2. Input vector \( x \in X \) randomly in the training set, and target class.
3. Initialize condition epoch=0
4. If (Epoch \( \leq \) MaxEpoch) and (\( \alpha \geq \) Min\( \alpha \))
   a. epoch=epoch +1
   b. for \( i = 1 \) to \( n \)
5. (1) determine \( j \) for \( D_i = \min \{D_i\} \quad i \in \{1, 2, \ldots, m\} \) for all \( i \)
6. (2) update \( W_i \)
\[
W_j = \begin{cases} 
W_j + \alpha(W_j - X) & \text{for } x \text{ correctly classified} \\
W_j - \alpha(W_j - X) & \text{for } x \text{ incorrectly classified} 
\end{cases}
\]

(3) Decrease \( \alpha \) with \( \alpha = \alpha \cdot \text{dec} \alpha \)

Since only the nearest weight vector is changed, this step can be interpreted as an additional supervised fine-tuning of the feature map once the neighborhood order is decreased to zero. This fine-tuning is useful if the decision surfaces of the classification are known and the classes covering its boundary classify inputs inside as well as outside of the boundary. In this case, it may be advisable to fine tune the position of the weight vectors with an LVQ algorithm such that safe and unsafe operating points are classified by different neurons.

3. RESEARCH METHOD

In the proposed clustering technique, the first step is to determine the coherent bus clusters. A contingency is considered such as load increase at all bus and outage of a line. To determine the coherency of buses, the sensitivity information such as voltage difference, angle difference, real and reactive load power differences are calculated. Using such sensitivity information as inputs to the Kohonen neural network, the coherent buses are grouped together to form several bus clusters. The buses in a cluster are coherent if the voltage, angle, real power and reactive power differences for each bus within a cluster are the same when subjected to a disturbance [7]. The results of bus clusters formed by using the Kohonen neural network are compared with the LVQ algorithm. Figure 1 shows the flowchart of the procedure for formation of bus clusters technique by using Kohonen NN.

As an input data a set of data namely Voltage (V), phase angle (\( \theta \)), Real Power (P) and Reactive Power (Q) at each bus in every contingency are taken from simulation results. Firstly, simulation running with an increasing all load bus by 25% in a step as contingency. The maximum cluster number determined by using coherency data (V, \( \theta \), P and Q) before voltage at a bus consider collapsed. This maximum cluster is then compared by using LVQ result. The test will be repeated by using other contingency such as line outages. A line from bus 3 to 4 will consider outages in order to get the maximum cluster number. Then maximum cluster for this contingency will be compare with LVQ result.

4. RESULTS AND DISCUSSION

To illustrate the effectiveness of the proposed method in forming the bus clusters, the coherency based clustering algorithm was applied to the IEEE 39-bus test system which consists of 17 load buses and 12 generator buses. Two contingencies were considered in the simulation of voltage collapse, namely, load increase at the load bus and line outage at a particular line.

In this case, for the load increase scenario, the loads at all the load buses were increased in steps of 25% p.u. MVA. All the loads are considered as voltage dependent loads. The simulation results are described as follows:

4.1. Formation of Bus Clusters Due to Load Increase

The results of clustering the 17 load buses and 12 generators buses of the 39 bus test system are shown in Table 1. The results show that the buses are grouped into 4 clusters in which all the buses in a cluster are said to be coherent. If the clusters are increased more than 4, it is noted that the performance of the Kohonen NN does not improve in which it still forms 4 clusters.
It can be seen that bus cluster number 3 consists of 21 coherent buses in one cluster. Both the Kohonen-NN and LVQ clustering techniques give similar results with regards to the number of clusters formed. The bus clusters formed for the 39 bus test system based on the Kohonen-NN is shown graphically as in Figure 2. The Kohonen-NN gives more freedom to determine the maximum number of clusters based on coherency of the buses rather than the LVQ in which the number of clusters are pre-determined depending on the representative buses that are selected.
4.2. Formation of Bus Clusters Due to Line Outage
The results for the formation of bus clusters when a line outage of line between bus 3 and 4 is considered is shown in Table 2 and Figure 3. Results in Table 2 show that the buses in the 39-bus test system are grouped into 3 coherent bus clusters due to the effect of a line outage of line between bus 3 and bus 4. By forming 3 bus clusters, the number of measurements can be reduced considerably to almost one third.
Table 2  Formation of bus clusters by using Kohonen-NN and LVQ line outage case

<table>
<thead>
<tr>
<th>Bus No</th>
<th>Kohonen-NN</th>
<th>LVQ</th>
<th>Type bus</th>
<th>Bus No</th>
<th>Kohonen-NN</th>
<th>LVQ</th>
<th>Type Bus</th>
</tr>
</thead>
<tbody>
<tr>
<td>6</td>
<td>1</td>
<td>1</td>
<td>PQ</td>
<td>37</td>
<td>2</td>
<td>2</td>
<td>PV</td>
</tr>
<tr>
<td>17</td>
<td>1</td>
<td>1</td>
<td>PQ</td>
<td>39</td>
<td>2</td>
<td>2</td>
<td>PV</td>
</tr>
<tr>
<td>23</td>
<td>1</td>
<td>1</td>
<td>PQ</td>
<td>10</td>
<td>3</td>
<td>3</td>
<td>PQ</td>
</tr>
<tr>
<td>24</td>
<td>1</td>
<td>1</td>
<td>PQ</td>
<td>11</td>
<td>3</td>
<td>3</td>
<td>PQ</td>
</tr>
<tr>
<td>26</td>
<td>1</td>
<td>1</td>
<td>PQ</td>
<td>13</td>
<td>3</td>
<td>3</td>
<td>PQ</td>
</tr>
<tr>
<td>27</td>
<td>1</td>
<td>1</td>
<td>PQ</td>
<td>14</td>
<td>3</td>
<td>3</td>
<td>PQ</td>
</tr>
<tr>
<td>28</td>
<td>1</td>
<td>1</td>
<td>PQ</td>
<td>15</td>
<td>3</td>
<td>3</td>
<td>PQ</td>
</tr>
<tr>
<td>29</td>
<td>1</td>
<td>2</td>
<td>PV</td>
<td>16</td>
<td>3</td>
<td>2</td>
<td>PQ</td>
</tr>
<tr>
<td>38</td>
<td>1</td>
<td>2</td>
<td>PQ</td>
<td>18</td>
<td>3</td>
<td>3</td>
<td>PQ</td>
</tr>
<tr>
<td>1</td>
<td>2</td>
<td>2</td>
<td>PQ</td>
<td>19</td>
<td>3</td>
<td>3</td>
<td>PQ</td>
</tr>
<tr>
<td>2</td>
<td>2</td>
<td>2</td>
<td>PQ</td>
<td>20</td>
<td>3</td>
<td>3</td>
<td>PQ</td>
</tr>
<tr>
<td>3</td>
<td>2</td>
<td>2</td>
<td>PQ</td>
<td>21</td>
<td>3</td>
<td>3</td>
<td>PQ</td>
</tr>
<tr>
<td>4</td>
<td>2</td>
<td>2</td>
<td>PQ</td>
<td>22</td>
<td>3</td>
<td>2</td>
<td>PQ</td>
</tr>
<tr>
<td>5</td>
<td>2</td>
<td>2</td>
<td>PQ</td>
<td>31</td>
<td>3</td>
<td>3</td>
<td>PV</td>
</tr>
<tr>
<td>7</td>
<td>2</td>
<td>2</td>
<td>PQ</td>
<td>32</td>
<td>3</td>
<td>3</td>
<td>PV</td>
</tr>
<tr>
<td>8</td>
<td>2</td>
<td>2</td>
<td>PQ</td>
<td>33</td>
<td>3</td>
<td>3</td>
<td>PV</td>
</tr>
<tr>
<td>9</td>
<td>2</td>
<td>2</td>
<td>PQ</td>
<td>34</td>
<td>3</td>
<td>3</td>
<td>PV</td>
</tr>
<tr>
<td>12</td>
<td>2</td>
<td>2</td>
<td>PQ</td>
<td>35</td>
<td>3</td>
<td>3</td>
<td>PV</td>
</tr>
<tr>
<td>25</td>
<td>2</td>
<td>2</td>
<td>PQ</td>
<td>36</td>
<td>3</td>
<td>3</td>
<td>PV</td>
</tr>
<tr>
<td>30</td>
<td>2</td>
<td>2</td>
<td>PV</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Figure 3. Bus Clusters Formed Due to Line Outage

5. CONCLUSIONS

Clustering a power system is very useful for the purpose of voltage stability control. By forming bus clusters the size of a power network is reduced and therefore the computational efficiency of application program such as voltage control can be considerably improved. The bus clusters are formed based on the coherent nature of buses in a cluster. To automate the process of forming the bus clusters, the Kohonen-NN which is based on an unsupervised training algorithm is proposed. The LVQ which is based on the supervised training algorithm is also implemented to compare it with the Kohonen-NN. The results showed that both the Kohonen-NN and LVQ techniques give similar results with regards to number of bus clusters.
formed. The proposed technique results showed four clusters on contingency load increased and three clusters online outage contingency on IEEE 39 bus system as shown by the LVQ

REFERENCES